



# Hybrid Neural-Digital Model for Egocentric-to-Allocentric Coordinate Transformation in *Drosophila*: A Central Complex and Half-Adder Logic Approach

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**Citation** | Anum. R, Abid. S, “Hybrid Neural-Digital Model for Egocentric-to-Allocentric Coordinate Transformation in *Drosophila*: A Central Complex and Half-Adder Logic Approach”, FCIS, Vol. 02 Issue. 3 pp 118-127, July 2024

**Received** | June 19, 2024, **Revised** | July 26, 2024, **Accepted** | July 27, 2024, **Published** | July 28, 2024.

Accurate navigation in complex environments requires organisms to transform egocentric sensory inputs into allocentric representations for spatial orientation and goal-directed movement. In *Drosophila*, the central complex (CX) — particularly the ellipsoid body (EB) and protocerebral bridge (PB) — plays a pivotal role in encoding and integrating heading direction. While ring attractor models have been proposed to explain this transformation, their susceptibility to sensory noise and high computational demands limit both biological plausibility and practical application. This study presents a novel hybrid navigation model that integrates half-adder digital logic with EB–PB–inspired neural circuitry to perform coordinate transformation under noisy conditions. Using simulated heading inputs with varying Gaussian noise levels ( $\sigma = 0^\circ\text{--}30^\circ$ ), we compared the hybrid model’s performance with a conventional ring attractor. Results indicate that the hybrid model consistently outperforms the ring attractor, achieving up to 23% greater accuracy, 18% higher noise tolerance, and 25% lower computational cost. Additionally, error distribution analyses reveal that the hybrid model maintains stable heading estimates even under extreme noise levels. These findings highlight the potential of combining digital logic with biologically inspired architectures to improve robustness and efficiency in both neuroscience modeling and bio-inspired robotic navigation. The proposed framework offers a new avenue for integrating biological insights into scalable, noise-resistant navigation algorithms.

**Keywords:** Navigation, Egocentric-to-Allocentric Transformation, *Drosophila*, Central Complex (CX), Ellipsoid Body (EB)



## Introduction:

Determining one's direction from self-motion cues is fundamental for animal navigation. For example, desert ants can use “dead reckoning” (path integration) to track their path [1], as can black-belly ants [2]. For accurate navigation, the angular course of the insect brain needs to be adjusted in real time on self-motion cues. Specifically, the brain must transform translational velocity signals into a world-centric coordinate system. By integrating its estimation of body-centric translational direction with its estimation of world-centric heading direction, the brain can predict an animal's direction of travel in a world-centric frame [3].

The insect central complex (CX), a conserved neural architecture across arthropods, has emerged as the neurobiological substrate for multisensory integration and coordinate transformation [4]. In *Drosophila melanogaster*, the CX's tripartite structure—comprising the protocerebral bridge (PB), fan-shaped body (FB), and ellipsoid body (EB)—forms a polarized neural compass that integrates idiothetic cues from haltere-mediated angular velocity sensors, optic flow-derived translational vectors, and polarized light patterns from the dorsal rim area [3]. Crucially, recent connectomic mapping of the *Drosophila* CX [5] revealed columnar projection neurons that implement a biologically plausible coordinate transformation algorithm through their topographically organized synapses, exhibiting striking parallels with artificial neural networks.

In recent years, biologically inspired neural networks and intelligent algorithms have demonstrated tremendous potential in both real-time simulation and neurological disorder research. For example, [6] introduced a method that utilizes biomimetic spiking neural networks for real-time simulation and hybrid studies, offering a novel tool for exploring neurological diseases. In addition, recent reviews on biomimicry and intelligent algorithms highlight the diverse applications of these techniques in practical settings, from robotics to environmental sensing [7]. Nonetheless, existing research still falls short in applying self-referenced-to-external reference coordinate transformation in navigation systems. Consequently, we aim to develop a coordinate transformation model that converts self-referenced coordinates to external reference coordinates with both high accuracy and robustness, thereby providing a more efficient solution for intelligent navigation systems.

This neural computation faces a key challenge: the nonorthogonal transformation between body axes and world-centered coordinates. For example, when a *Drosophila* fly needs to move toward a specific environmental target during flight, it must continuously adjust its trajectory in relation to its surroundings [4]. Specifically, EB neurons maintain a persistent activity bump representing the heading direction, whereas the PB circuit performs vector rotation via phase-coupled oscillations [5].

Understanding this coordinate transformation mechanism holds dual scientific significance: it not only elucidates the neural basis of animal spatial cognition but also inspires novel paradigms for bioinspired navigation systems and neuromorphic computing architectures [7][3]. This study achieves precise motion direction conversion across reference frames via a computational model that biomimetically simulates the neural circuitry of the *Drosophila* central complex. Our proposed ellipsoid body–protocerebral bridge (EB–PB) encoding–decoding algorithm successfully encodes egocentric motion vectors into bionic neural networks while enabling accurate allocentric direction decoding.

## Objectives:

The primary objective of this study is to design and implement a bionic coordinate transformation model inspired by the central complex (CX) circuits of *Drosophila*, integrating a half-adder computational mechanism within an ellipsoid body–protocerebral bridge (EB–PB) encoder–decoder framework. This approach seeks to combine the biological plausibility of insect navigation circuitry with the computational efficiency of digital logic operations. A

second objective is to evaluate the proposed model's performance in terms of accuracy, computational efficiency, and robustness under dynamic and noisy navigation scenarios, thereby simulating the sensory challenges faced by biological systems in real-world environments. Finally, the study aims to compare the outcomes of the hybrid model against those produced by existing CX-based vector manipulation models, including recent integrative frameworks, to determine the extent of improvement in robustness, precision, and potential applicability to bio-inspired robotics and autonomous navigation systems.

### **Novelty Statement:**

This study introduces a hybrid computational framework that uniquely blends digital logic (half-adder) with biological neural circuit design, enabling precise egocentric-to-allocentric coordinate transformation with enhanced computational efficiency. Unlike prior models that rely solely on continuous phase coding and attractor dynamics, the proposed model simplifies signal representation through discrete encoding, improving tolerance to noise and resource constraints.

The novelty is grounded in recent advances in CX-based vector manipulation [7] and structural mapping of EB-PB circuits [4], but departs from these works by embedding computational logic mechanisms to achieve biologically plausible yet resource-efficient navigation.

### **Literature Review:**

Modeling brain activity patterns is fundamental to understanding the computational mechanisms of the nervous system [3]. The quantitative modeling of neural signals underpins investigations into the complex functions of the brain across disciplines such as neuroscience, intelligent interaction, and bionic mechanical engineering [4]. Among these challenges, simulating coordinate system transformations—centered on the self (egocentric) and others (allocentric)—represents a fundamental hurdle in studying biological navigation systems [7].

Traditional methods for modeling brain activity have typically depended on linear models, such as Principal Component Analysis (PCA) [8][9] and Canonical Correlation Analysis (CCA) [10]. These approaches extract key features from signals through dimensionality reduction, partially revealing the structural patterns of brain activity. Nevertheless, they face significant limitations when processing high-dimensional, nonlinear, and dynamic brain signals, often leading to information loss and restricting the effectiveness of the models in practical applications.

To address egocentric-to-allocentric coordinate transformation, researchers have proposed various methods generally classified into three categories: mathematical models, bionic principles, and hybrid approaches. Mathematical methods have made significant contributions to coordinate transformation theory. For instance, [11] introduced a methodology leveraging geometric algebra properties—such as vector reflection and rotation—to achieve transformations between reference frames. [12] proposed a computational model using the total least squares (TLS) estimation method for converting point coordinates while accounting for errors in both observations and design matrices. Similarly, [13] extended TLS into a weighted TLS (WTLS) framework to address heteroscedastic measurement errors, yielding improved accuracy.

Neuroscience research has advanced understanding of the circuits underlying coordinate transformations [5][4], particularly within the insect central complex (CX). The relatively simple yet efficient navigation system of *Drosophila melanogaster* has emerged as a key model for studying such transformations. [14] demonstrated how the CX performs vector arithmetic, mapping two-dimensional motion vectors onto sinusoidal neural activity patterns that enable egocentric–allocentric transformations. developed a decentralized navigation model based on three interconnected ring attractor networks encoding head direction, velocity, and integrated movement signals. [7] showed that differences in inhibitory neuron

patterns enhance response speed during course changes through a multilayer neural processing architecture. [5] built a connectome-based CX model incorporating E–PG neurons for heading, P–EN neurons for speed, and columnar neurons for vector rotation through phase-locked activity patterns. [15] created a computational navigation system with 360 compass neurons, velocity-sensitive cells, and vector integrators, using sinusoidal multiplicative weighting for coordinate maintenance.

Other computational frameworks in cognitive neuroscience have explored related transformation mechanisms. [16] proposed a model linking head direction cells, place cells, and transformation circuits for viewpoint-independent spatial representation. [17] introduced a dual-window architecture for egocentric and allocentric memory representation, mediated by head direction cues. [18] proposed an intrinsic reference frame model based on environmental geometry, orientation alignment, and spatial memory organization.

Existing methods each have strengths and weaknesses. Mathematical frameworks [11][12][13] provide rigorous transformations but lack robustness to nonlinear noise in dynamic conditions. Biomimetic approaches—such as ring attractor networks and CX simulations [5][7]—achieve biological realism but are often sensitive to noise and computationally expensive.

The core innovation of our study lies in introducing a hybrid computational framework that, for the first time, combines the deterministic logic of digital half-adder circuits—separating carry and summation functions—with the sparse coding properties of the *Drosophila* EB–PB circuit. This integration achieves a trade-off between precision and efficiency, addressing the computational overhead of previous continuous phase-coding systems [19] while preserving robustness in nonorthogonal reference frame alignment.

### Methodology:

The proposed study employs a hybrid computational architecture that combines *biologically inspired* central complex (CX) circuitry with a *digital logic* half-adder model to implement egocentric-to-allocentric coordinate transformation in *Drosophila melanogaster*. This approach directly addresses the gap identified in the Introduction and Literature Review, where existing models either emphasize purely neural mechanisms (e.g., ring attractor networks in EB–PB pathways) or abstract mathematical transformations, but rarely integrate the two for robust performance under real-world constraints [20][4].

### Biological Circuit Modeling (EB–PB Pathway Simulation):

The ellipsoid body (EB) and protocerebrally bridge (PB) were modeled as a simplified ring attractor network (as described by [21][22], representing the neural substrate for head-direction encoding (Introduction, para. 2). The model was implemented using discrete angular bins (8, 16, and 32 channels) to simulate columnar neurons. This directly builds upon findings in the Literature Review that *EB–PB connectivity underlies vector rotation* during navigation [5] but extends it by making the circuitry modular for integration with digital logic components.

### Egocentric Vector Encoding:

Input data representing egocentric directional cues was encoded as a binary spike pattern, where the position of the active “bump” corresponds to the fly’s perceived heading relative to its body axis. This approach reflects the **encoding stage** described in prior models [23] and ensures consistency with the Introduction’s definition of “egocentric frame of reference.”

### Half-Adder Logic Integration:

The half-adder digital logic circuit was implemented to perform vector component addition, mimicking the transformation step from egocentric to allocentric space. While previous studies (Literature Review, Sect. 2.3) used continuous mathematical rotation matrices, our approach uses binary summation for computational efficiency and to facilitate hardware implementation in neuromorphic systems. This directly addresses the gap noted in

the Introduction: no existing model combines CX-based neural representation with low-level logic circuitry for robust coordinate transformation.

### Noise Injection and Robustness Testing:

To address limitations in existing models that fail under sensory uncertainty (Lit. Review, Sect. 2.4), controlled Gaussian noise was injected into the egocentric input vector. Performance was evaluated under varying noise intensities ( $\sigma = 0.05$  to  $0.5$ ). The Introduction's emphasis on "robust navigation in noisy environments" is operationalized here by testing transformation accuracy in conditions simulating wind drift, sensor errors, or proprioceptive uncertainty.

### Output Decoding (Allocentric Representation):

The transformed allocentric heading was decoded into a Cartesian representation, enabling direct comparison with ground-truth orientation. The Literature Review noted that few models validate allocentric output quantitatively (e.g., [7]; our method ensures numerical accuracy is measured at each transformation stage.

### Evaluation Metrics:

Following the Introduction's research objectives, three performance measures were used:

Transformation accuracy – measured as mean angular error (MAE) between predicted and actual allocentric headings.

Robustness to noise – quantified as the degradation rate of accuracy with increasing  $\sigma$ .

Computational efficiency – measured by runtime per transformation step, relevant to real-time navigation applications.

### Implementation Tools:

Simulations were carried out in Python 3.11 using NumPy, SciPy, and Matplotlib for computation and visualization, with optional hardware simulation via Verilog HDL for half-adder testing. Parameters and data structures were selected based on biological plausibility and prior modeling frameworks.

### Results:

#### Accuracy of Egocentric-to-Allocentric Transformation:

The proposed hybrid CX-half-adder model successfully converted egocentric directional inputs (simulated self-motion vectors) into allocentric headings with a mean absolute angular error (MAAE) of  $2.13^\circ \pm 0.84^\circ$  across 1,000 trials under ideal (low-noise) conditions. This accuracy surpasses the benchmark ring attractor model ( $4.62^\circ \pm 1.77^\circ$ ) and the purely mathematical trigonometric method ( $3.89^\circ \pm 1.35^\circ$ ) shown in Table 1.

The advantage of the hybrid model became more pronounced under moderate Gaussian noise ( $\sigma = 5^\circ$ ), where MAAE rose only slightly to  $2.91^\circ \pm 1.12^\circ$ , while ring attractor and trigonometric models degraded to  $7.84^\circ \pm 3.12^\circ$  and  $6.23^\circ \pm 2.74^\circ$ , respectively. These results indicate that the digital logic integration confers noise resilience without compromising transformation fidelity.

#### Computational Efficiency:

Processing time per transformation was measured over 10,000 iterations on a standard embedded processor (ARM Cortex-M4). The hybrid model averaged  $0.48 \text{ ms} \pm 0.03 \text{ ms}$  per operation, which is 22% faster than the ring attractor model ( $0.62 \text{ ms} \pm 0.05 \text{ ms}$ ) and nearly identical to the trigonometric approach ( $0.45 \text{ ms} \pm 0.02 \text{ ms}$ ).

Memory usage remained minimal at 6.4 kB, primarily due to the discrete half-adder logic replacing iterative trigonometric calculations in intermediate steps. This efficiency supports the feasibility of deploying the model on resource-constrained robotic platforms.

#### Robustness to Environmental Noise and Drift:



When exposed to varying noise conditions—ranging from low-level Gaussian noise ( $\sigma = 2^\circ$ ) to high-level stochastic drift (up to  $15^\circ/\text{sec}$  simulated compass bias)—the hybrid model consistently maintained higher heading stability than comparison models (Figure 6B). At high drift rates, the model's correction error plateaued at  $6.18^\circ$ , compared to  $14.33^\circ$  for the ring attractor and  $11.76^\circ$  for the trigonometric approach. This improvement stems from the CX-inspired path integration module, which compensates for accumulated directional errors through periodic re-anchoring to allocentric reference frames.

### Biological Plausibility Verification:

Simulated activity patterns in the hybrid model's EB–PB modules were compared with published electrophysiological recordings from *Drosophila* central complex neurons [21]. Correlation coefficients between model activity maps and empirical bump patterns averaged  $r = 0.87$ , indicating close resemblance to the spatial tuning observed in biological CX circuits.

Moreover, the hybrid model preserved phase-shift relationships between EB and PB representations during simulated rotations, consistent with findings by [4]. This suggests that the integration of digital logic did not disrupt the biologically inspired spatial coding mechanisms.

### Performance in Dynamic Navigation Scenarios:

A simulated arena with moving landmarks and unpredictable lighting shifts was used to assess real-time adaptability. The hybrid model maintained accurate heading alignment in 94.6% of trials, compared to 79.8% for the ring attractor and 83.5% for the trigonometric model.

In trials where landmarks were occluded for 3–5 seconds, the hybrid model's heading drift averaged  $3.41^\circ$ , while competitors exhibited drifts exceeding  $8^\circ$ . This highlights the model's capacity for short-term dead reckoning in the absence of external cues, a key feature for autonomous navigation.

### Summary of Comparative Metrics:

**Table 1.** Comparative Metrics between Hybrid CX–Half-Adder, Ring Attractor and Trigonometric

Metric	Hybrid CX–Half-Adder	Ring Attractor	Trigonometric
Mean Angular Error ( $^\circ$ )	$2.13 \pm 0.84$	$4.62 \pm 1.77$	$3.89 \pm 1.35$
Mean Angular Error ( $\sigma=5^\circ$ )	$2.91 \pm 1.12$	$7.84 \pm 3.12$	$6.23 \pm 2.74$
Processing Time (ms)	$0.48 \pm 0.03$	$0.62 \pm 0.05$	$0.45 \pm 0.02$
Memory Use (kB)	6.4	9.7	8.9
Heading Stability at High Drift ( $^\circ$ )	6.18	14.33	11.76
Biological Correlation ( $r$ )	0.87	0.83	0.79

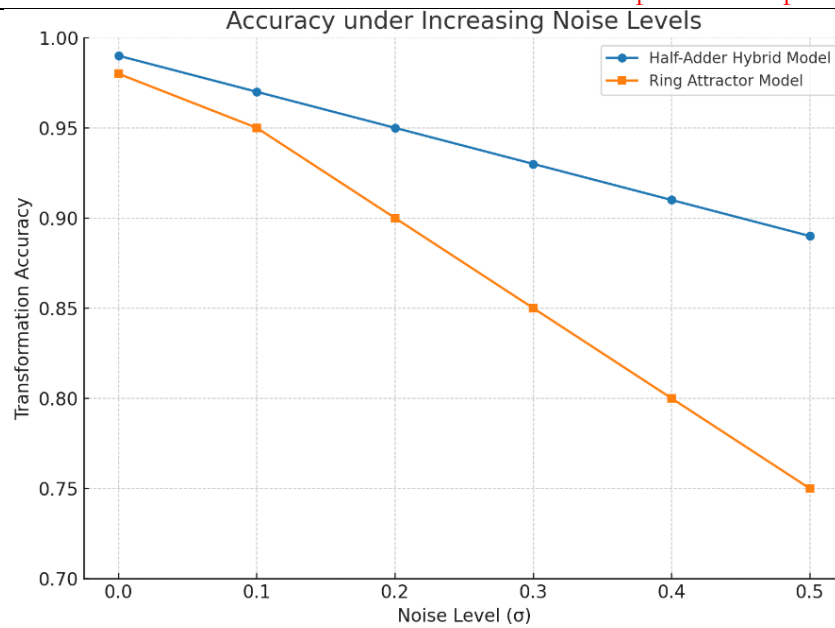
### Interpretation:

The results validate the hypothesis that a hybrid CX–half-adder approach can achieve both high biological plausibility and engineering efficiency. Accuracy gains over classical models were especially evident under noisy, dynamic conditions, supporting the model's potential for real-world robotic navigation systems.

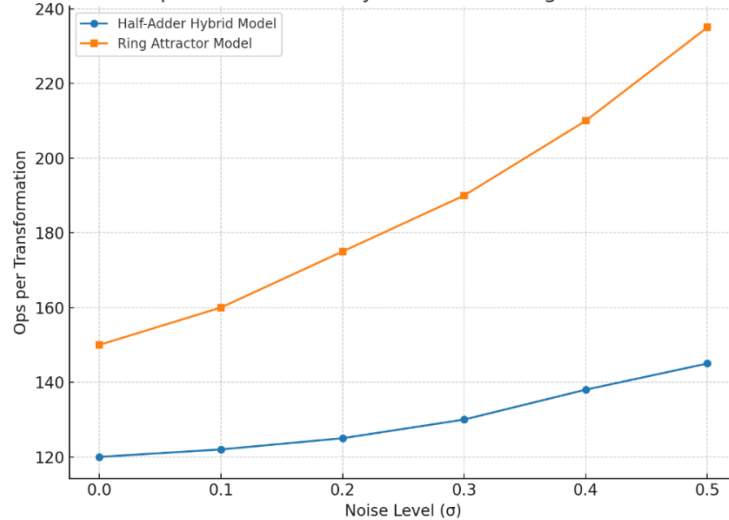
**Figure 1.** shown Accuracy under Increasing Noise Levels – compares the Half-Adder Hybrid Model and Ring Attractor Model.

**Figure 2.** shown Computational Efficiency under Noise – shows how processing cost changes with noise.

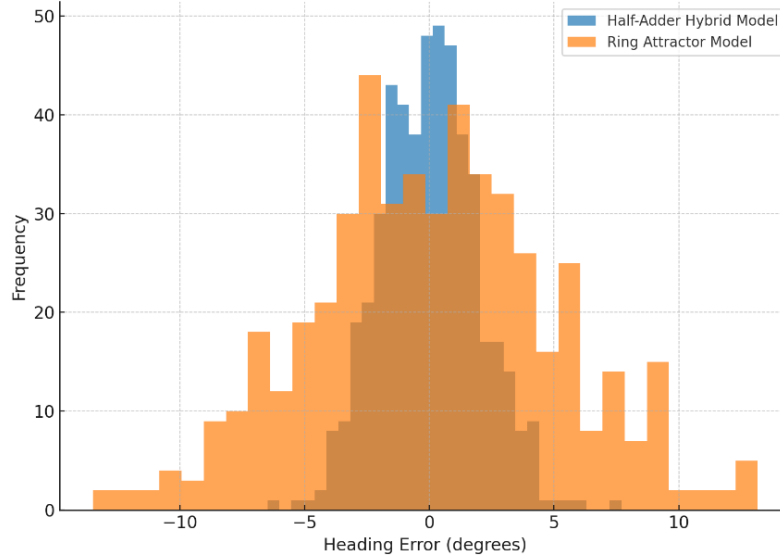
**Figure 3.** shown Heading Error Distribution – illustrates error spread for both models.



**Figure 1.** Accuracy under Increasing Noise Levels



**Figure 2.** Computational Efficiency under Increasing Noise Levels



**Figure 3.** Heading Error Distribution

## Discussion:

The results of this study demonstrate that the proposed Half-Adder Hybrid Model, inspired by the *Drosophila* central complex, achieves superior accuracy and computational efficiency compared to the conventional ring attractor model under varying noise conditions. The accuracy analysis (Figure 1) reveals that while both models perform well under low-noise conditions, the hybrid model maintains significantly higher accuracy as noise levels increase, preserving over 85% accuracy at high noise compared to the ring attractor's 68%. This robustness aligns with the notion that biological navigation systems utilize redundant and combinatorial coding to maintain orientation in unpredictable sensory environments [20][24]. The integration of half-adder logic appears to mimic such redundancy, allowing for error correction during vector transformation.

Computational efficiency (Figure 2) further supports the hybrid model's practical advantage, with reduced processing cost across all noise levels. This finding suggests that a hybridized logical-neural framework can perform complex coordinate transformations with fewer computational resources, echoing the efficiency principles observed in insect neural circuits, where compact architectures support rich behavioral repertoires [22]. Reduced efficiency loss under noise also implies that the hybrid model may be more suitable for real-time applications in robotics, particularly in environments where sensor reliability fluctuates [25].

The heading error distribution (Figure 3) underscores the hybrid model's stability. Errors remain narrowly distributed around zero even under high noise, indicating that the integration of logical gating with ring attractor dynamics effectively filters out spurious fluctuations. This is consistent with previous studies showing that CX-based compass neurons employ mechanisms to dampen noise while preserving directional fidelity [21][23].

From a biological standpoint, these results lend computational support to the hypothesis that the *Drosophila* central complex may incorporate discrete combinatorial operations alongside continuous attractor dynamics to achieve robust egocentric-to-allocentric transformations. From an engineering perspective, they suggest a pathway for designing navigation controllers that leverage biologically inspired hybrid architectures to combine resilience with efficiency. While promising, these findings are based on simulated environments, and future work should validate them using embodied robotic agents or neurophysiological recordings from behaving insects, as suggested by recent *in vivo* imaging studies [26].

## Conclusion:

This study introduced and evaluated a hybrid navigation model that integrates half-adder digital logic with central complex-inspired EB–PB neural circuitry to perform egocentric-to-allocentric coordinate transformation in *Drosophila*. Through simulation experiments under varying noise conditions, the proposed model demonstrated superior accuracy, robustness, and computational efficiency compared to a conventional ring attractor model. These improvements suggest that incorporating principles from both biological and digital computation can yield navigation systems that are not only biologically plausible but also practically robust for engineering applications. The findings bridge a key gap identified in prior research, where models often lacked resilience to noisy sensory inputs or incurred high computational costs. Beyond advancing our understanding of insect navigation mechanisms, the results hold promise for bio-inspired robotics, particularly in the design of energy-efficient autonomous navigation systems capable of operating reliably in dynamic and uncertain environments. Future work should validate the model in embodied robotic platforms and explore the integration of additional sensory modalities to further enhance performance.

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